**Binary search tree. Removing a node**

Remove operation on binary search tree is more complicated, than add and search. Basically, in can be divided into two stages:

* search for a node to remove;
* if the node is found, run remove algorithm.

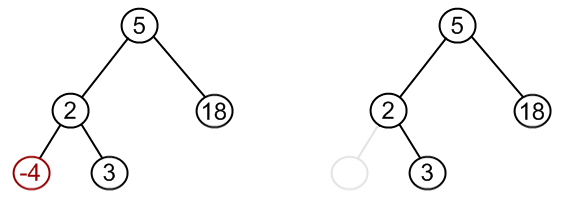
**Remove algorithm in detail**

Now, let's see more detailed description of a remove algorithm. First stage is identical to [algorithm for lookup](http://www.algolist.net/Data_structures/Binary_search_tree/Lookup), except we should track the parent of the current node. Second part is more tricky. There are three cases, which are described below.

1. Node to be removed has no children.

This case is quite simple. Algorithm sets corresponding link of the parent to NULL and disposes the node.

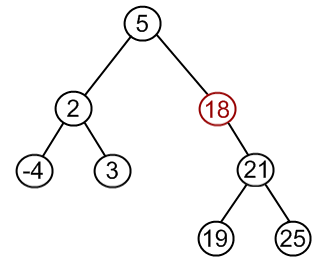
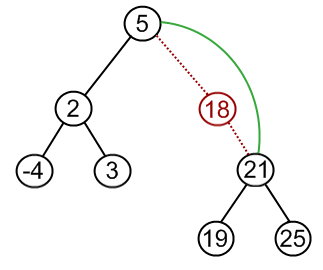
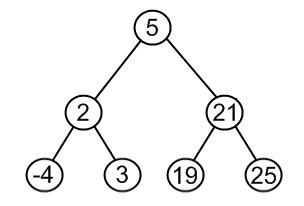
**Example.**Remove -4 from a BST.



1. Node to be removed has one child.

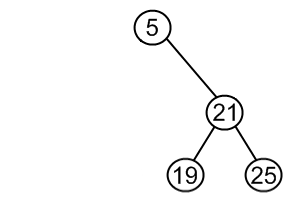
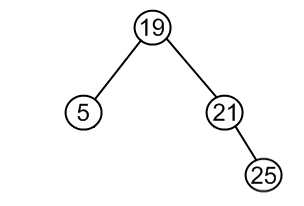
It this case, node is cut from the tree and algorithm links single child (with it's subtree) directly to the parent of the removed node.

**Example.**Remove 18 from a BST.

1. Node to be removed has two children.

This is the most complex case. To solve it, let us see one useful BST property first. We are going to use the idea, that the same set of values may be represented as different binary-search trees. For example those BSTs:

  
  
contains the same values {5, 19, 21, 25}. To transform first tree into second one, we can do following:

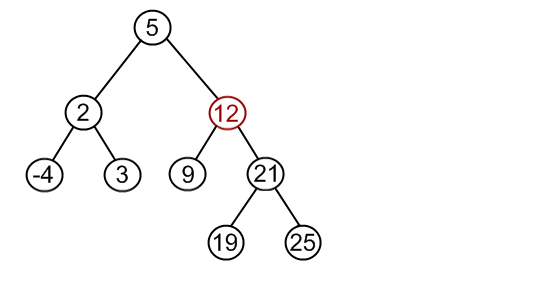
* + choose minimum element from the right subtree (19 in the example);
  + replace 5 by 19;
  + hang 5 as a left child.

The same approach can be utilized to remove a node, which has two children:

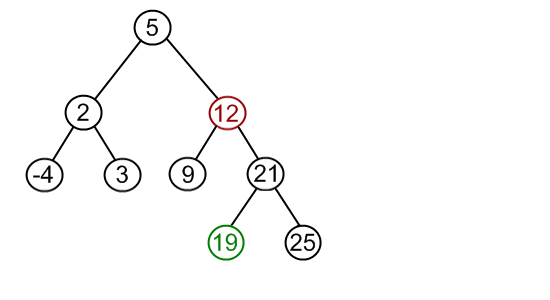
* + find a minimum value in the right subtree;
  + replace value of the node to be removed with found minimum. Now, right subtree contains a duplicate!
  + apply remove to the right subtree to remove a duplicate.

Notice, that the node with minimum value has no left child and, therefore, it's removal may result in first or second cases only.

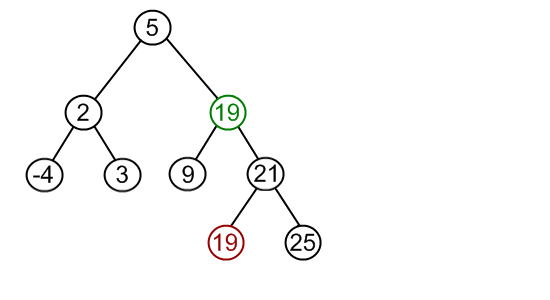
**Example.**Remove 12 from a BST.



Find minimum element in the right subtree of the node to be removed. In current example it is 19.



Replace 12 with 19. Notice, that only values are replaced, not nodes. Now we have two nodes with the same value.



Remove 19 from the left subtree.

